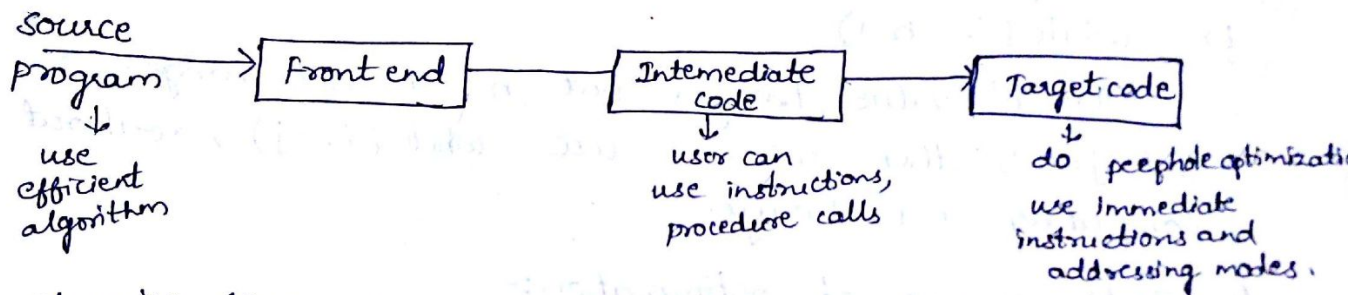


CODE OPTIMIZATION

Code Optimization:-

Code optimization is required to produce efficient target code. There are 2 important issues that need to be considered, while applying the code optimization,

- i.) Semantic equivalence of source program, should not be changed
- ii.) Program efficiency must be achieved without changing the algorithm of source program.



Classification of optimization:-

- 1.) Machine dependent optimization
- 2.) Machine independent optimization

Machine dependent optimization:-

It is based on the characteristics of the target machine for the instruction set used and addressing modes used for the instruction to produce the efficient target code.

- Allocation of sufficient number of resources.
- Using immediate instruction whenever necessary.

Machine Independent Optimization:-

It is based on the characteristics of programming languages for a appropriate programming structure and usage of efficient arithmetic properties in order to generate efficient code.

- i.) From the source program eliminate unreachable code.
- ii.) Use alternative equivalent sequence of instructions that will produce efficient target code.
- iii.) Move two or more identical computations at one place and make use of the result instead of each time computing the expressions.

Ex:- while($i <= n-1$)

Here 'i' value changes but $n-1$ does not change. So let $j = n-1$, then we can use while($i <= j$), without computing $n-1$ always.

Principle Sources of optimization:-

1) Common Sub expression Elimination:-

An expression 'E' is called common sub expression if it was previously computed and the values of the variables in expression 'E' have not change since previous computation. In this we have to avoid recomputing of the expression, if its value is already being computed.

Ex:-

$t_1 := 4 \times i$
 $n := a[t_1]$
 $t_2 := 4 \times i$
 $t_3 := 4 \times j$
 $t_4 := a[t_3]$
 $a[t_2] := t_4$
 $t_5 := 4 \times j$
 $a[t_5] := n$

After
elimination
→

$t_1 := 4 \times i$
 $n := a[t_1]$
 $t_3 := 4 \times j$
 $t_4 := a[t_3]$
 $a[t_1] := t_4$
 $a[t_3] := n$

The result of both is same but difference is we eliminate repeated statements in RHS.

2) Copy Propagation:-

It means use of one variable instead of another variable. If $x := y$ is a copy statement then copy propagation is a kind of transformation in which use 'y' for 'x', whenever possible, after copy statement $x := y$.

Ex:-

$n := t_1$
 $a[t_1] := t_2$
 $a[t_3] := n$

→

$n := t_1$
 $a[t_1] := t_2$
 $a[t_3] := t_1$

3) Constant folding:-

In which the constant expressions are calculated during the compilation. Here the value of expression is a constant and using the constant, do the constant folding.

Ex:-

$\text{const max} := 3$
 $i := 2 + \text{max}$
 $j := 2 \times 3 + a$

→

$i := 5$
 $j := 6 + a$

4) Dead code elimination:-

A variable is said to be live in the program if its value can be used in the program.

otherwise it is said to be dead at that point.
So, optimization can be performed by eliminating such a dead code.

Ex:-
t := false
if (t)
{
 ==
 ==
}

- One advantage of copy propagation is that it often turns copy statement into dead code. Hence after the copy propagation if dead-code elimination is done, then useless statements can be removed.
- Optimization can be done in 2 places in the program.
 - i) local optimization
 - ii) Global optimization.

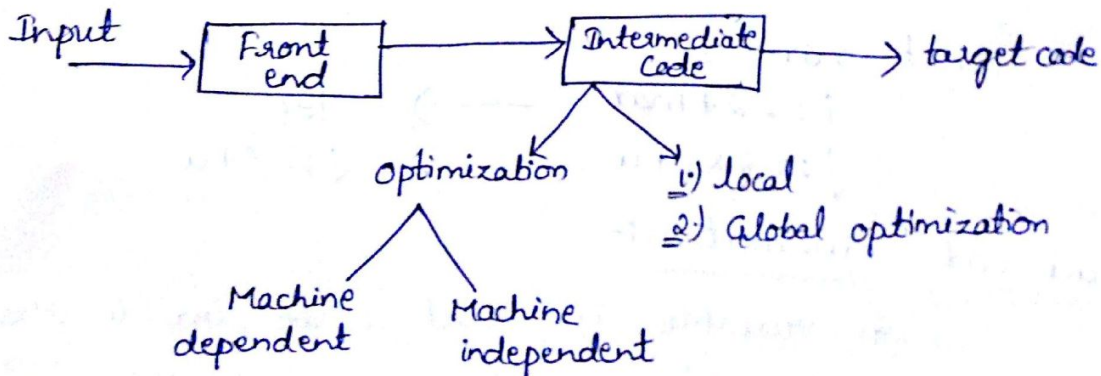
i) Local optimization :-

Local optimization can be done within the block in the program.

ii) Global optimization :-

Global optimization can be done throughout the program.

Loop Optimization :-



- The code optimization can be significantly done in loops.

The inner loops where the program spend bulk amount of time, so the running time of the program may be improve, if we decrease the number of instructions in inner loop, even if we increase the amount of instructions outside the loop.

Loop optimization can be carried out by the following methods:

- 1) Code motion.
- 2) Induction variable
- 3) Strength Reduction
- 4) Loop invariant method
- 5) Loop unrolling
- 6) Loop fusion.

1. Code motion:-

code motion is a technique, which moves the code outside the loop.

<p><u>Ex:-</u> while($i < \text{limit} - 2$)</p> <pre>{ --- }</pre>	<p>→</p>	<pre>t = limit - 2; while($i < t$) { --- }</pre>
---	----------	--

2. Induction variable:-

A variable 'x' is called Induction variable of the loop 'L' if the value of the variable gets change in every time. It is either increment or decrement by some constant

<p><u>Ex:-</u></p> <pre>i := i + 1 t1 := 4 * i t2 := a[t1] if $t2 < 10$ goto B1</pre>	<p>→</p>	<pre>t1 := t1 + 4 t2 := a[t1] if $t2 < 10$ goto B1</pre>
---	----------	--

Here 'i' and 't1' variables are induction variables.

3. Strength Reduction:-

Here the strength of certain operators is higher than the others. For example, the strength of * operator is higher than + operator. In this we can replace * with + operator.

Ex:- for(i=1; i<=100; i++)
{
 count := i * 7;
}

→

```
temp = 7;  
for(j=1; j<=100; j++)  
{  
  count = temp;  
  temp = temp + 7;  
}
```

4. Loop Invariant Method:-

Here the computation of instructions inside the loop is avoided and thereby the computation overhead of the compiler is avoided.

Ex:- while(i <= 50)
{
 i := i + a/b;
}

→

```
t = a/b  
while(i <= 50)  
{  
  i = i + t;  
}
```

5. Loop Unrolling:-

Here the number of testing conditions and jumping instructions can be reduced by using executing the code 2 times.

Ex:- while(i <= 50)
{
 a[i] = b[i];
 i++;
}

→

```
while(i <= 50)  
{  
  a[i] = b[i];  
  i++;  
  a[i] = b[i];  
  i++;  
}
```

6. Loop Fusion:-

Here several loops in program is merged into single loop.

Ex:- for i = 1 to n do
 for j = 1 to m do
 a[i,j] = 0;

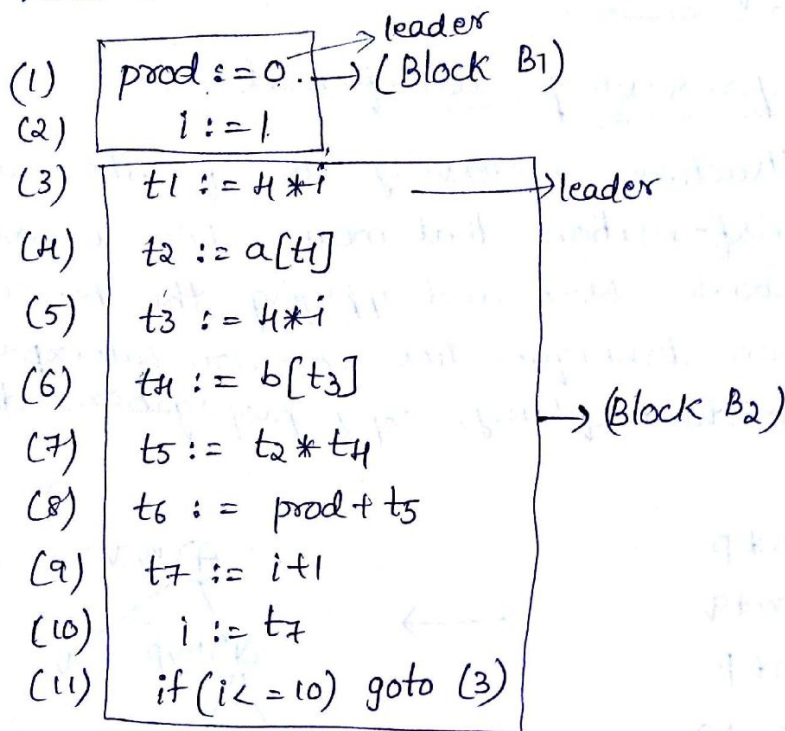
→

```
for i = 1 to n * m do  
  a[i] := 0;
```

Basic Block:-

Basic block is a sequence of consequent statements in which flow of controls entered at begin and ending at last without halting the program or possibility of branching is called Basic block.

Ex:- Find out the basic blocks on 3-address code.



Optimizing basic blocks:-

- 1) structure preserving transformation (by using DAG).
- 2) use algebraic identities.

Terminologies use in basic blocks:-

1. Define and use
2. Live and Dead variables.

Algorithm for partitioning into basic blocks:-

1. At first, we are determining leaders from the basic block.
2. The first statement or the first instruction in

m
T

the intermediate code or basic block is a 'leader'.

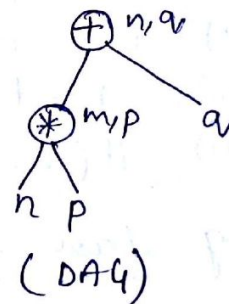
3. Any statement that immediately follows 'goto' or unconditional goto is called a leader.
4. The basic block formed by set of instructions from the starting leader to the next leader in the intermediate code.

Optimization of Basic blocks:-

1. Structure preserving transformations:-

Structure preserving transformation is a DAG based transformation that means DAG is constructed from the basic block and applying the principal sources of optimization techniques like common subexpression elimination, constant folding, copy propagation, dead code elimination.

Ex:-
 $m := n * p$
 $n := m + q$
 $p := n * p$
 $q := m + q$



• Here the common subexpressions are $m := n * p$ and $n := m$ that are identified from the DAG and eliminate the common subexpressions.

2. Use of Algebraic Identities:-

i-) The algebraic transformations can be obtained using strength reduction technique.

Ex:- Instead of $2 * a$ we can use $a + a$ and instead of $a / 2$ we can use $0.5 * a$.

ii-) Now the constant folding technique can be applied to achieve the algebraic transformations.

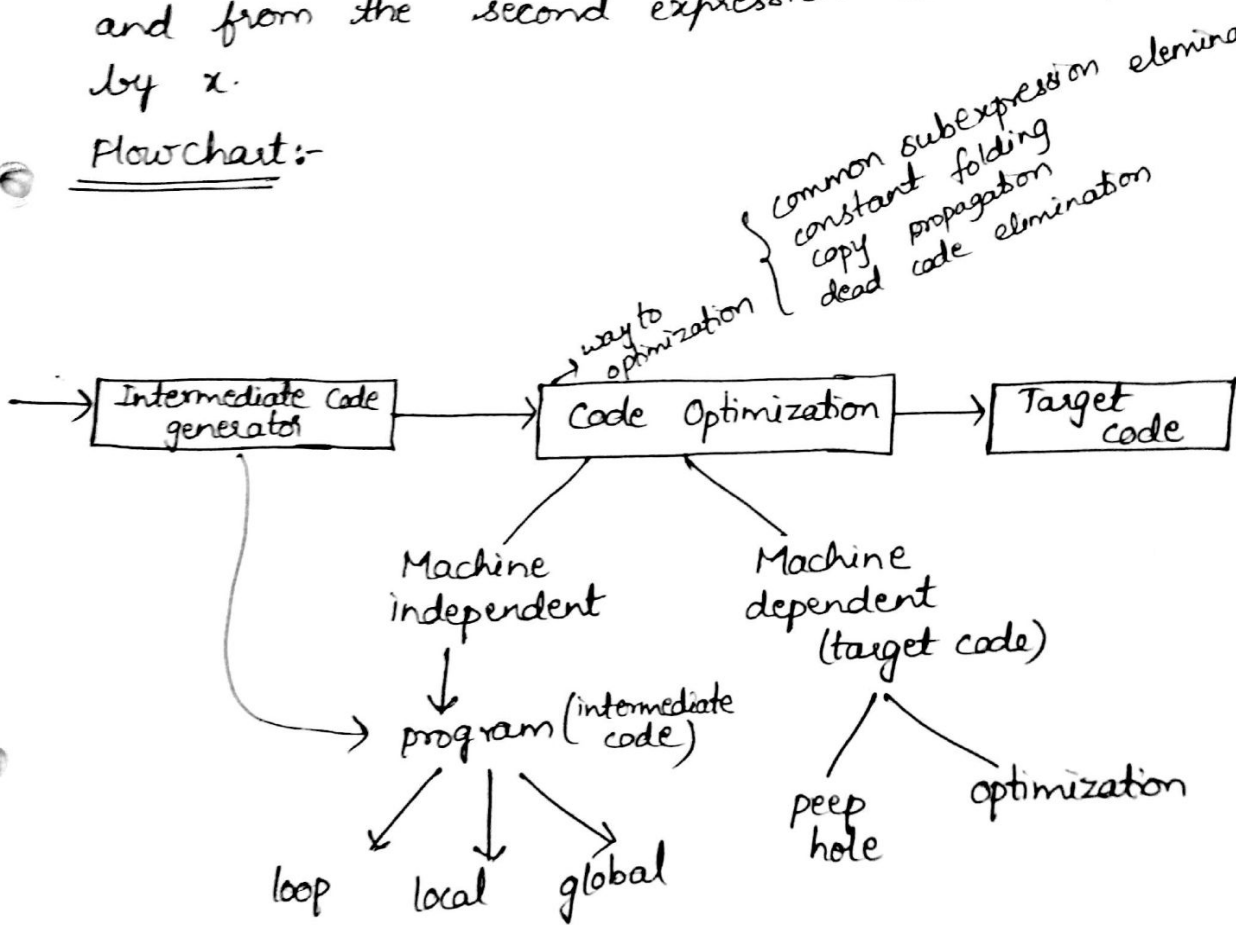
EX:- Instead of using $x := 2 * 3 * 14$ we can use $x := 6 * 28$

iii.) The use of common subexpression elimination, we use associativity and commutativity is to apply algebraic transformations on basic blocks.

EX:- $x := y * z$
 $t := z * r * y$

• Here commutative law can be applied as $y * z = z * y$ and from the second expression we can replace $z * y$ by x .

Flowchart:-



Peephole Optimization:-

Here optimization can be done on target program which is generated by the compiler.

Characteristics of peephole optimization:-

1. Redundant instruction elimination
2. Flow of control optimization
3. Algebraic simplification

4. Reduction in strength

5. Use of machine Idioms.

- Peephole is nothing but it is a simple window, is moved over the target program and applied the optimization.

1. Redundant instruction elimination:-

Here redundant instructions are the redundant loads and redundant stores can be eliminated in this type of transformation.

Ex:- MOV R₀, X

MOV X, R₀

Here MOV X, R₀ is a redundant instruction because the value of X is already in register R₀.

2. Flow of control optimization:-

Here unnecessary jumps can be eliminated using peephole optimization unnecessary jumps or jumps can be eliminated.

Ex:- goto test

test: goto done

done:

goto done

done:

3. Algebraic Simplification:-

Peephole optimization is an effective technique for algebraic simplifications. The statements such as $x = x + 0$ and $x = x * 1$ can be eliminated in target program by using peephole optimization.

4. Reduction in strength:-

Here certain operators or certain machine instructions

are cheaper than the other in order to improve efficiency of target program, we can replace these instructions by cheaper instructions.

Ex:- x^2 is cheaper than $x*x$, and addition, subtraction instructions are cheaper than multiplication and division. So, we can effectively use equivalent addition and subtraction for multiplication and division.

5) Use of Machine Idioms:-

Here target instructions have equivalent machine instructions for performing some of the operations, hence we can replace these target instructions by equivalent machine instructions in order to improve efficiency of target program.

Ex:- Some machines having auto increment and auto decrement instructions or addressing modes are used to perform addition and subtraction operations. Eg: `progcount`

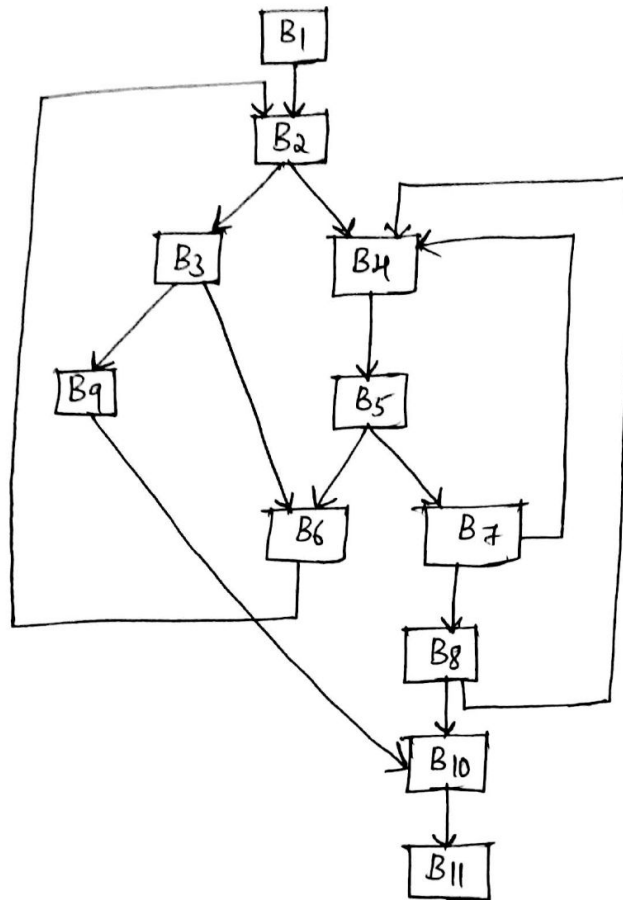
Flow Graph:-

- Flow graph is a directed graph in which flow of control information is added to the basic blocks, the nodes to the flowgraph are represented by basic block.
- So, the block whose leader is first statement is called Initial block. There is a directed edge from block B_1 to block B_2 , if B_2 immediately follows B_1 in sequence, we can say that B_1 is predecessor of block B_2 .

Loops in the Flow Graph:-

- Ex:- Consider the following flow graph and find
- a. Denominators for each basic block.
 - b. Detect all loops in the graph.

For each loop find the back edge and header block information.



Sol:- a.)

- B1: dominates all block
- B2: itself
- B3: B9
- B4: B4, B7, B8
- B5: B7, B8
- B6: itself
- B7: B8
- B8: itself
- B9: itself
- B10: B11
- B11:

Backedge B6-B2

header: B2

Backedge B7-B4

header: B4

Backedge B8-B4

header: B4

Loops in the Flow Graph:-

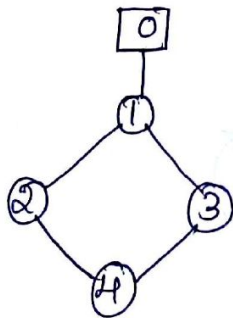
Loop is a collection of nodes in the flow graph.

1. All such nodes are strongly connected that means always there is a path from any node to any another node within that loop.
2. The collection of nodes have unique entry, that means there is only one path from a node outside the loop to a node inside the loop.

Basic Terminologies:-

1. Denominators:- In a flow graph a node 'd' denominates 'n' if every path to node 'n' from initial node goes to 'd' only. This can be denoted as ' $d \text{ dom } n$ '. Every initial node denominates all the nodes in the flowgraph.

Ex:-

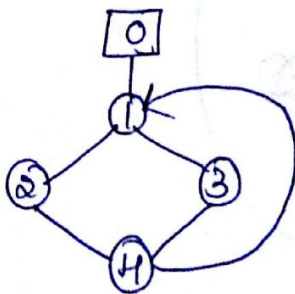


Here block '0' dominates all nodes in flow graph.

2. Natural loops:-

Loop in a flow graph can be denoted by $n \rightarrow d$ such that 'd' dominates 'n'. These edges are called back edges and for a loop there can be more than one back edges. If there is $P \rightarrow Q$ then 'Q' is head and 'P' is tail and head dominates tail.

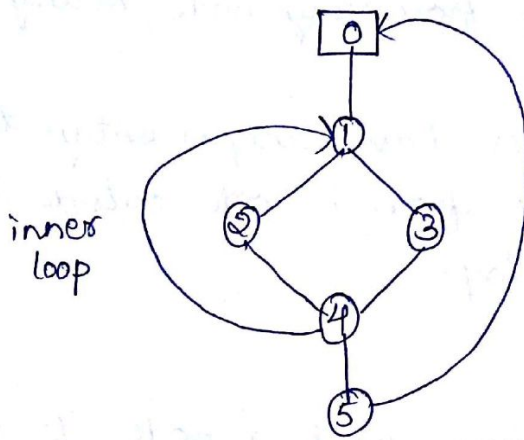
Ex:-



3) Inner Loops:-

The inner loop is a loop that contains no another loop.

Ex:-

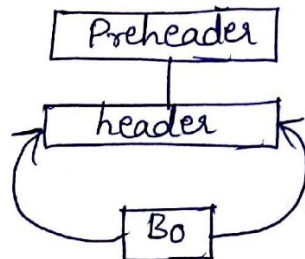


1-4 (inner loop)
4-1 (backedge)

4. Preheaders

Preheader is a new block created such that successor of this block is header and the all the computations that can be made before the header block.

Ex:-



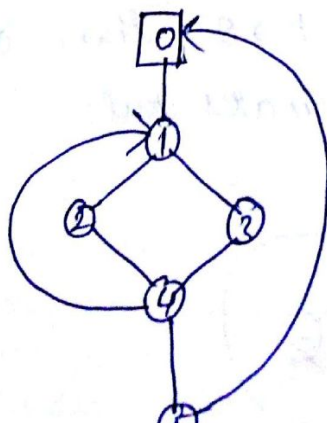
5. Reduceable Flow graphs

There are 2 types of flow graphs, forward edges and backward edges. These edges have following properties:

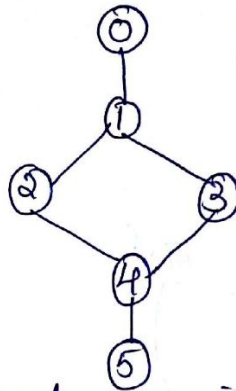
i) Forward edges from a acyclic graph.

ii) Backward edges are edges whose head dominates their tail

Ex:-



Backward edges are $5 \rightarrow 0$ and $4 \rightarrow 1$ and reduce or eliminate backward edges from the flow graph. Now the flow graph can be represented as



- The program structure, in which there is exclusive use of if-else statement, while loop or goto statements generates flowgraph which is always reducible.

Local optimization:-

The optimization done using DAG-

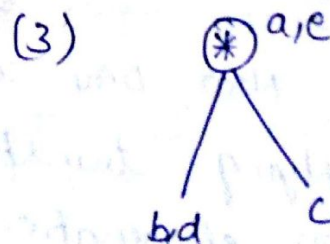
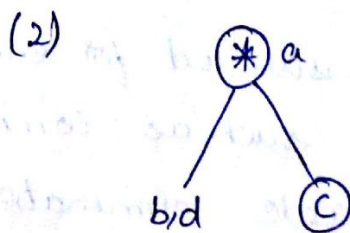
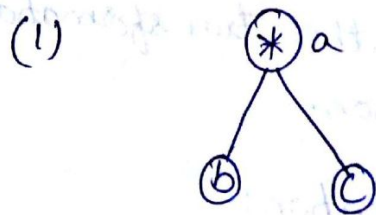
Ex:-

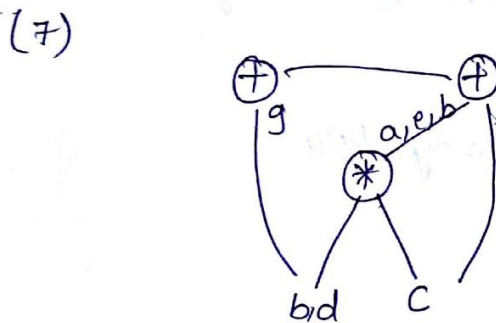
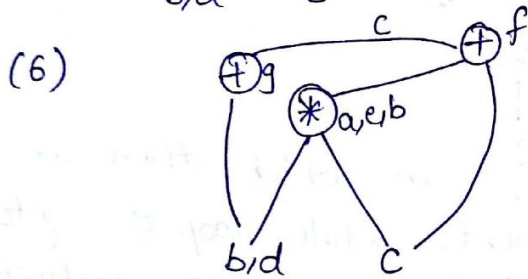
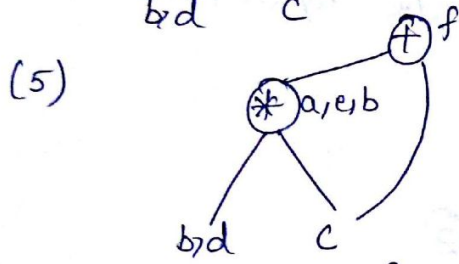
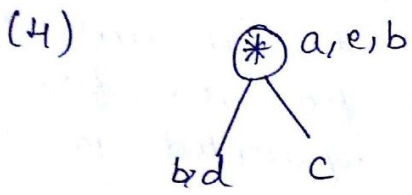
```

a := b * c
d := b
e := d * c
b := e
f := b + c
g := f + d
  
```

Block B₁

Sol:- The DAG for first instruction in block is as follows





Local optimization :-

The local optimization is done at a restricted scope. Local optimization is a kind of optimization that can be done on some sequence of statements involving or available in basic block. New DAG is constructed for basic block and applying the transformation techniques for doing local optimization.

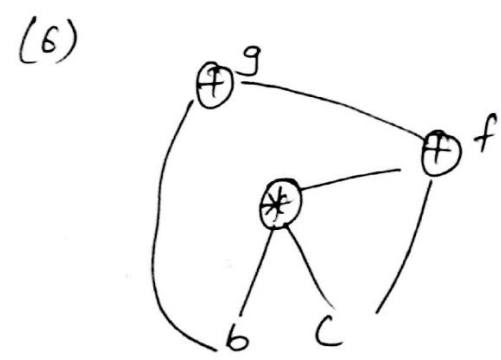
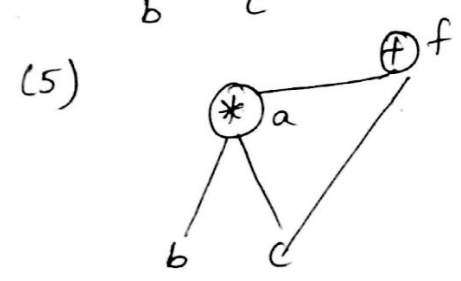
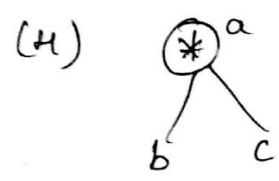
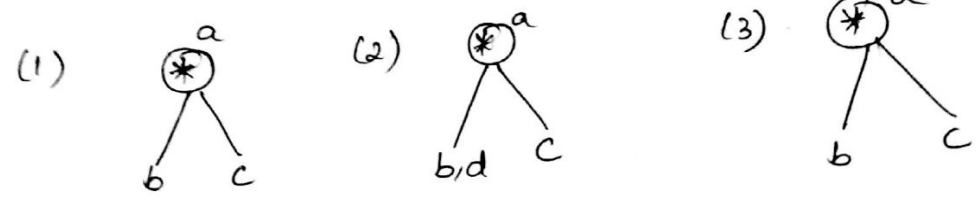
DAG based local optimization :-

New DAG can be constructed for each block and applying transformations such as common sub expression elimination, dead code elimination, copy propagation, constant folding; For performing the

Local optimization, new optimization can be generated by using DAG.

- i.) Common subexpression $e := d * c$ which is actually $b * c$ is eliminated since $d := b$.
- ii.) Deadcode statements like $b := e$ is eliminated.

Ex:



```

a := b * c
d := b
f := a + c
g := f + d
    
```

Global optimization:-

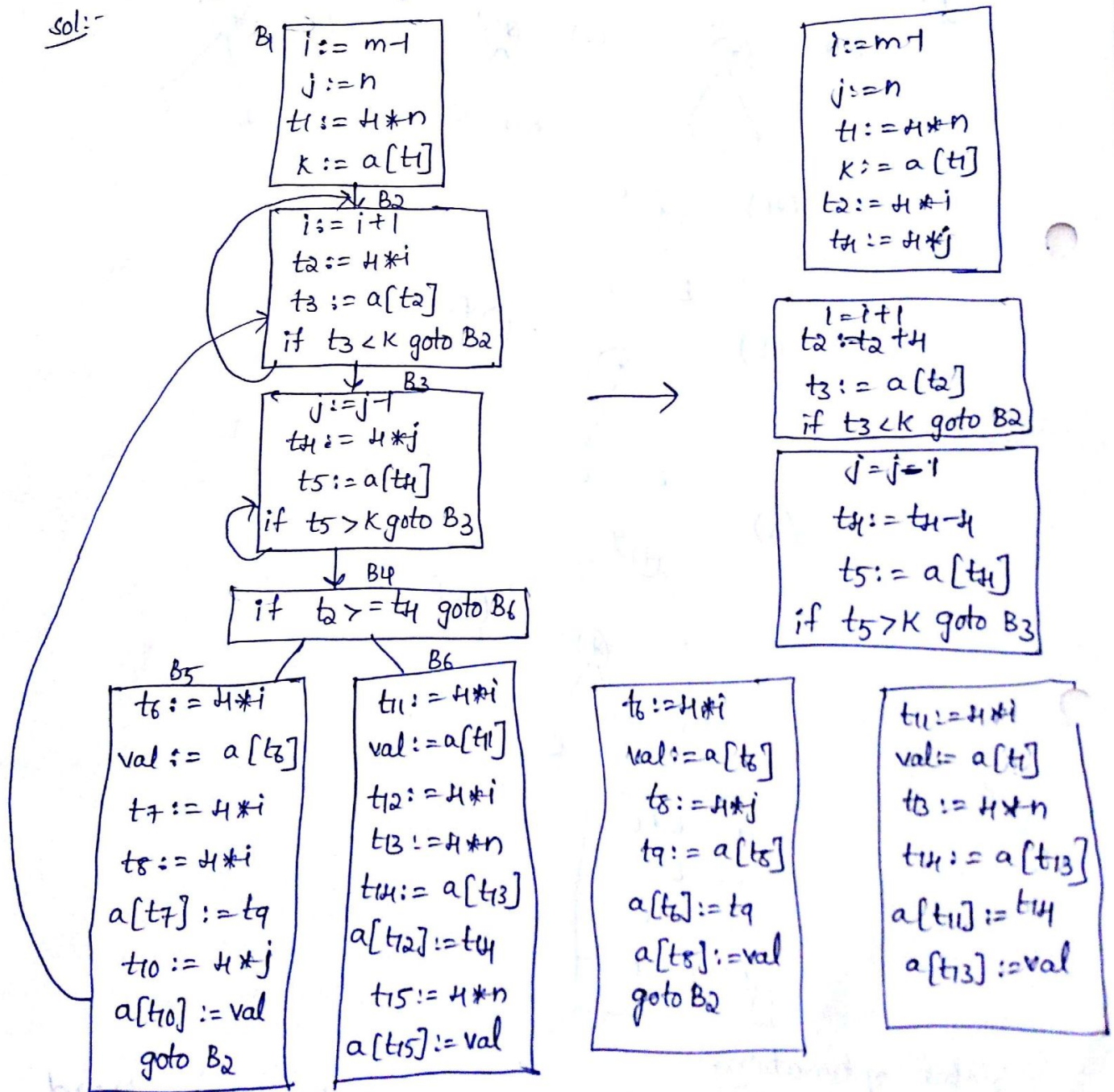
Global optimization is applied over a broad scope such as function (or) procedure (or) flowgraph.

- For a global optimization, program is represented

in the form of program flow graph. So, the program flow graph is a graphical representation in which each node is a block and edges represents flow of control from one block to another block.

Ex:- Compare the local optimization with global optimization.
Give some example.

Sol:-



B5

```

val := a[t2]
t9 := a[t4]
a[t2] := t9
a[t4] := val

```

D6

```

val := a[t2]
t4 := a[t4]
a[t2] := t4
a[t4] := t3

```

• Two types of global optimization analysis

1. Control flow analysis
2. Data flow analysis

1. Control Flow Analysis:-

The control flow analysis determines the information regarding arrangement of graph nodes, presence of loops and nesting of loop and nodes visited before execution of specific node. So, thus in control flow analysis the analysis made on flow of control by carefully examining the program in flow graph.

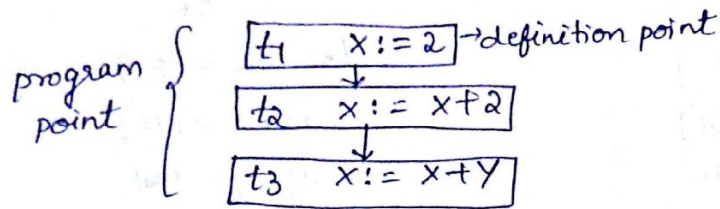
2. Data flow analysis:-

Data flow analysis is an analysis made of the data flow. So, that is the data flow analysis, determines the information regarding definition and use of the data in program. So, the data flow analysis is basically a process in which the values are computed using data flow properties. Here the properties are

- i. Available expression
- ii. Reaching definition
- iii. Live and Dead variables
- iv. Busy expression.

• Some of the common terminologies in the program

are definition point, reference point and evaluation point.



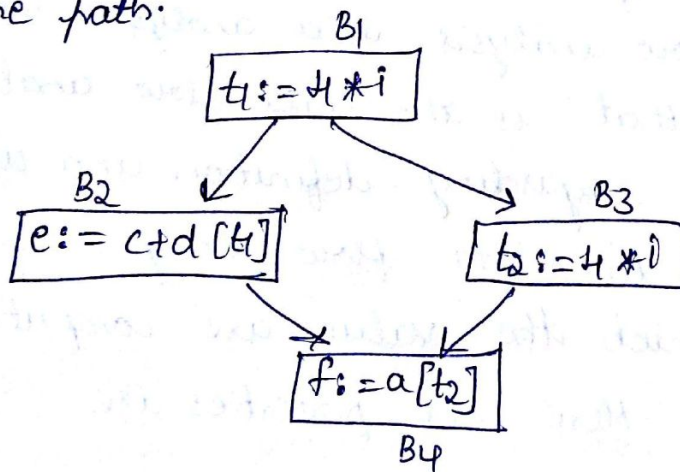
- A program point containing definition is called definition point
- A program point at which reference to a data item is called reference point.
- A program point at which some evaluating expression is given is called as evaluation point.

i.) Available Expression:-

A expression $x+y$ is available at program point

w if and only if along all the paths reaching to w .

- The expression $x+y$ is said to be available at its evaluation point.
- The expression $x+y$ is said to be available if no definite of any operand of expression follows its last evaluation along the path.



- Here expression $4 * i$ is available expression for block B_2, B_3, B_4 , because this expression is not been changed by any of block before appearing in block B_4

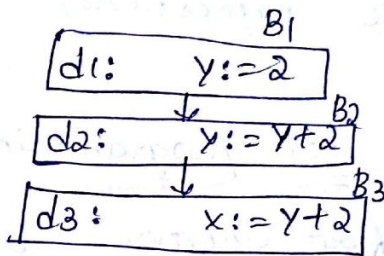
Advantage:-

- Easy to eliminate common sub expressions.

ii.) Reaching Definitions:-

The definition d' reaches at point p' if there is a path from ~~past~~ D to P , along which D' is not killed.

- An definition D' of variable x' is killed when there is a redefinition of x' .
- So the definition d_1 said to be 'reaching definition' for block B_2 but definition d_1 is said to be not reaching definition for block B_3 because the value y' variable is killed in block B_2 .



Advantage:-

- Used in constant and variable propagation.

iii.) Live Variables:-

A variable x' is live at some point p' , if there is a path from p' to exit along which the value of x' is used before it is redefined, otherwise the variable is said to be dead at some point.

Advantages:-

- Live variables are used to deadcode elimination and register allocation.

iv.) Busy Expression:-

A expression E' is said to be a busy expression along some path P_i to P_j iff and only if

an evolution of 'E' exists along some path P_i to P_j and no definition of any operand exists before its evolution along the path.

Advantage:-

- Useful in performing code movement optimization.

Data Flow Equations:-

Data flow Equations are the equations that are representing the expressions that are appearing in flow graph. These equations are useful for computing live variable, available expressions, and reaching definitions.

Data Flow Equations for programming constructs:-

The data flow equation written in a form of equation such that,

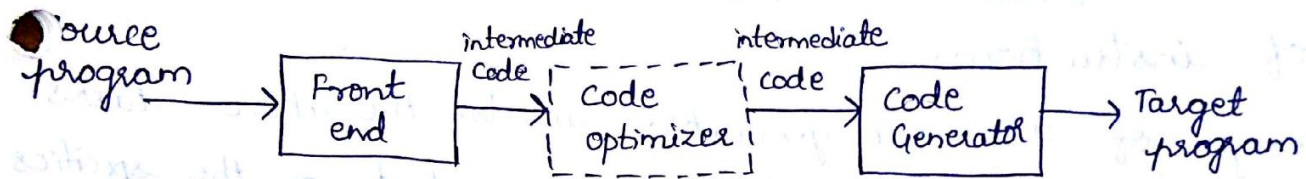
$$\begin{array}{ccc} \text{out}[s] = \text{gen}[s] \cup (\text{in}[s] - \text{kill}[s]) \\ \downarrow & & \downarrow \\ \text{synthesized} & & \text{inherited} \\ \text{attributes} & & \text{attributes} \end{array}$$

- Here 's' stands for the statement for which the data flow equation can be written.
- 'out' represents output i.e., the information generated at the end of the statement.
- 'gen' stands for generating the information within the statement and
- 'in' represents gathered information before entering into the loop,

CODE GENERATION

Code Generation Phase:-

- Final phase in compiler model
- Takes as input intermediate representation (IR) code symbol table information.
- produces output semantically equivalent target program.



- Compiler needs to produce efficient target programs.
- Includes an optimization phase prior to code generation.
- May make multiple passes over the IR before generating the target program.

Target Program Code (or) Object code forms:-

- The back end code generator of a compiler may generate different forms of code depending on the requirements.
- Absolute machine code (executable code) - for small programs generate this code.
- Relocatable machine code (object files for linker) - using linker, compiler links subroutines.
- Assembly language (facilitates debugging) - in form of opcodes and addressing codes.
- Byte code forms for interpreters (Ex:- JVM)

Code generation phase:-

Code generation has 3 primary tasks:-

- Instruction selection:-
Choose appropriate target machine instructions to implement the IR (intermediate representation) statements.
- Register allocation and assignment:-
Decide what values to keep in which registers.
- Instruction ordering:-
Decide in what order to schedule the execution of instructions.
- Design of all code generators involve the above 3 tasks. Details of code generation are dependent on the specifics of IR, target language and run-time system.

The target Machine:-

- Implementing code generation requires thorough understanding of the target machine architecture and its instruction set.
- Our machine is byte-addressable (word = 4 bytes), has n -general purpose registers R_0, R_1, \dots, R_{n-1} .
- 2-address instructions of form instruction, opcode(source) destination data fields.

Ex:- opcodes (op)

MOV (move content from destination)

ADD

SUB

The Target Machine: Address modes:-

mode	form	Address	Added cost
Absolute	M	M	1
Register	R	R	0
Indexed	(CR)	C + contents(R)	1
Indirect register	*R	contents(R)	0
Indirect indexed	*(CR)	contents(C + contents(CR))	1
literal	#C	N/A	1

Instruction costs:-

- Machine is a simple processor with fixed instruction costs.
- cost of instruction = 1 + cost(source - mode) + cost(destination - mode).

Ex:-

Instruction	Operation	Cost
MOV R ₀ , R ₁	store content (R ₀) into register R ₁ (1+0+0)	1
MOV R ₀ , M	store content (R ₀) into memory location M (1+0+1)	2
MOV M, R ₀	store content (M) into register R ₀ (1+1+0)	2
MOV H(R ₀), M	store content (H + contents(R ₀)) into M (1+1+1)	3
MOV *(H(R ₀)), M	store content (contents(H + contents(R ₀))) into M (1+1+1)	3
MOV #1, R ₀	store content 1 into R ₀ (1+1+0)	2
ADD H(R ₀), *R(R ₁)	store content into (R ₀) add contents (H + contents(R ₀)) to value at location contents(R + contents(R ₁)) (1+1+1)	3

Instruction Selection:-

- Instruction selection is important to obtain efficient code.
- Suppose we translate 3-address code.

Ex:-
 $x := y + z$
 to: MOV Y, R0
 ADD Z, R0
 MOV R0, X

$a := a + 1 \Rightarrow$

MOV a, R0 (1+1+0)	2
ADD #1, R0	3
MOV R0, a (1+0+1)	2
cost = $\frac{7}{\downarrow}$	

<u>Better</u>	<u>Best</u>
⇓	⇓
(1+1+) ADD #1, a cost = 3	INC a cost = 2

Therefore in above example replace ADD #1, R0 with INC R0, so that cost can be reduced.

$a := a + 1 \Rightarrow$

MOV a, R0 (1+1+0)	2
INC R0	2
MOV R0, a (1+0+1)	2
cost = $\frac{6}{\underline{\quad}}$	

Need for Global Machine-specific code optimization:-

- Suppose we translate 3-address code

$x := y + z$
 to: MOV Y, R0
 ADD Z, R0
 MOV R0, X

Classes of storage in processor :-

Then we translate,

a := b + c	→	MOV a, R0	
d := a + e		ADD b, R0	
		MOV R0, a] redundant
		MOV a, R0	
		ADD e, R0	
		MOV R0, d	

Register Allocation and Assignment:-

- Efficient utilization of the limited set of registers is important to generate good code.
- Registers are assigned by
 - Register allocation to select the set of variables that will reside in registers at a point in the code.
 - Registers assignment to pick the specific register that a variable will reside in.
- Finding an optimal register assignment in general is NP-complete.

Ex:-

t := a * b
t := t + a
t := t / d

↓ {R1 = t}

MOV	a,	R1	}
MUL	b,	R1	
ADD	a,	R1	
DIV	d,	R1	
MOV	R1,	t	

Here we use only one register and only 5 instructions.
So, it is efficient.

Ex 2:-

$t := a * b$
 $t := t + a$
 $t := t / d$



{ R₀=a, R₁=t }

MOV a, R₀
MOV R₀, R₁
MUL b, R₁
ADD R₀, R₁
DIV d, R₁
MOV R₁, t

Here, we use 2 registers, and 6 instructions.
So, it is not efficient.

- Number of registers usage should be less to have an efficient output (target program).

Choice of Evaluation order:-

- When instructions are independent, their evaluation order can be changed.

Ex:-

$a + b - (c + d) * e \Rightarrow$
 $t_1 := a + b$
 $t_2 := c + d$
 $t_3 := e * t_2$
 $t_4 := t_1 - t_3$

reorder ⇓

$t_2 := c + d$
 $t_3 := e * t_2$
 $t_1 := a + b$
 $t_4 := t_1 - t_3$

MOV a, R₀
ADD b, R₀
MOV R₀, t₁
MOV c, R₁
ADD d, R₁
MOV e, R₀
MUL R₁, R₀
MOV R₁, R₀
SUB R₀, R₁
MOV R₁, t₄

MOV c, R₀
ADD d, R₀
MOV e, R₁
MUL R₀, R₁
MOV a, R₀
ADD b, R₀
SUB R₁, R₀
MOV R₀, t₄

Two classes of storage in processor :-

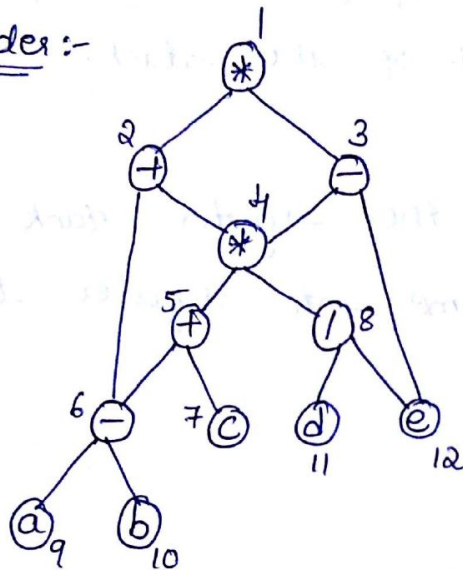
1. Registers :-

- Fast access, but only few of them
- Address space, not visible to programmer
- Doesnot support pointer access.

2. Memory :-

- slow access, but large
- supports pointers.

Heuristic order :-



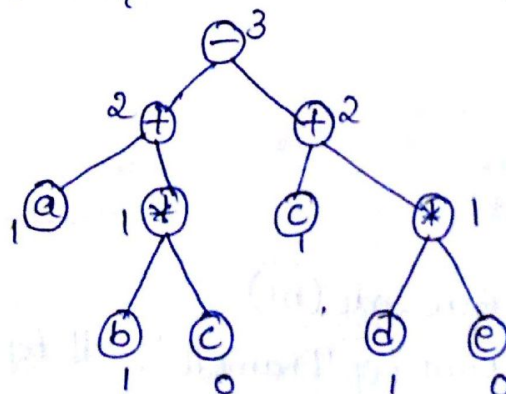
1, 2, 3, 4, 5, 6, 8 (except leaf nodes)

- By using this order of evaluation, efficiency of code generation is done maximum.

Labelling Algorithm :- (bottom up passion)

$$\text{label}(n) = \begin{cases} \max(L_1, L_2) & \text{if } L_1 \neq L_2 \\ L_1 + 1 & \text{if } L_1 = L_2 \end{cases}$$

Ex:- consider a DAG




Left → 1
right → 0

- Here we use data structure register stack, temporary stack. It contains general purpose registers R_0, R_1, \dots, R_{n-1} used while evaluation of expression, we push values to stack. The top of stack contains R_0 only. It contains temporary variables.
- It contains a function cod_gen(n). Its purpose is to generate a target code using information present in top of stack.
- Another function is swap functions. Its purpose is to swap registers in top of the stack.

case 1:

If the top of the register stack contains name, means load the name into register that can be obtained by


 print(MOV || name ||, top(reg.stack))

case 2:

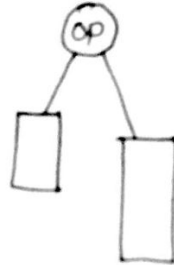
If the nodes right child is leaf n_2 , then, the target code will be, generate code for n_1 and then gen_code(n_2).



Gen_code(n_1)
 print(op || name || ', ' || top(regstack))

Case-3:

If the left child of n i.e., n_1 requires less number of registers than n_2 , then we swap the top two registers on top of stack.



Case-4:

If the both child requires same number of registers, then we evaluate first right sub-tree and store in temporary stack and then evaluate left sub-tree.